Architecture-Driven Modernization (ADM): Software Metrics Meta-Model (SMM)

FTF - Beta 1

OMG Document Number:  ptc/2009-03-03
Standard document URL:  http://www.omg.org/spec/SMM/1.0/PDF
Associated File(s)*:  http://www.omg.org/spec/SMM/20080501
                       http://www.omg.org/spec/SMM/20080601

* Original file(s):  XMI (admtf/08-05-05), XSD (admtf/08-06-05)

This OMG document replaces the submission document (admtf/08-05-04, Alpha). It is an OMG Adopted Beta Specification and is currently in the finalization phase. Comments on the content of this document are welcome, and should be directed to issues@omg.org by April 1, 2009.

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Preface

OMG

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- CORBA facilities
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• OMG Embedded Intelligence specifications
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**Typographical Conventions**

The type styles shown below are used in this document to distinguish programming statements from ordinary English. However, these conventions are not used in tables or section headings where no distinction is necessary.

Times/Times New Roman - 10 pt.: Standard body text

**Helvetica/Arial - 10 pt. Bold:** OMG Interface Definition Language (OMG IDL) and syntax elements.

**Courier - 10 pt. Bold:** Programming language elements.

**Helvetica/Arial - 10 pt:** Exceptions

**NOTE:** Terms that appear in italics are defined in the glossary. Italic text also represents the name of a document, specification, or other publication.


1 Scope

This specification defines a meta-model for representing measurement information related to software, its operation and its design. Referred to as the Software Metrics Meta-model (SMM), this specification is an extensible meta-model for exchanging software-related measurement information concerning existing software assets (designs, implementations, or operations). A standard for the exchange of measures is important given the role that measures play in software engineering and design.

The SMM include elements representing the concepts needed to express a wide range of software measures. The specification does include a library of software measures, but it is not asserting that the listed measures constitute standards themselves. Software measurement field is fairly young especially with respect to modernization. As the field matures, the measures considered as standard are likely to change.

The SMM is instead a specification for the definition of measures and the representation of their measurement results. The library serves to demonstrate the specification and provide a representation for many currently popular software measures.

The SMM is part of the Architecture Driven Modernization (ADM) roadmap and fulfills the metric needs of the ADM roadmap scenarios and as well as other information technology scenarios.

The SMM specifies the representation of measures without detailing the representation of the entities measured. SMM anticipates that those entities are represented in other OMG meta-models. Measures of software artifacts or their features that are defined within the SMM, the Knowledge Discovery Metamodel (KDM), the Abstract Syntax Tree Metamodel (ASTM), another ADM roadmap meta-model, or another OMG meta-model may arise as:

- Counts. (Lines of code measures exemplify the mechanism.)
- Direct applications of named measurements. (One such named measure is Cyclomatic Complexity.)
- Simple algebraic change of scales of already defined numeric measures (e.g., the translation to ‘choice points’ from Cyclomatic complexity).
- Simple algebraic aggregations of numeric artifact features, including other measures, over sets of software artifacts. (Determining the complexity of an application by summing the complexities of the application’s elements demonstrates this process.)
- Simple range-based grading or classification of already defined numeric measures. (Cyclomatic reliable/unreliable quadrants are one such a grading.)
- Qualitative evaluations where the range of evaluations can be mapped to a linear order.

Useful metrics must go beyond static (or dynamic) code analysis and technical performance to include factors related to information utility and acceptance of the system by the organization(s) participating in an enterprise. To be objective and repeatable, such metrics need to be based on technical characteristics of the system. Given a meta-model representation of such characteristics, the SMM will facilitate the exchange of such measures.

Given the evolutionary nature of system development and the predicate value of metrics with respect to “downstream” problems, metrics are gathered into trends or viewed from historical perspective. As shown in Section 14, SMM addresses the issues of trend and history to model for system development as long as the historical links of the measured entities are provided.

Consistent with other models defined by OMG, the SMM will be defined using the MOF meta-modeling language. As such, it will have a standard textual representation presented by XMI. Consequently, the exchange of metrics defined by SMM will be in the XMI. These models will, similarly, be compatible with MOF repositories for storage and retrieval by various tools.
2 Conformance

The principle goal of SMM is the exchange of measurements about software. To be SMM compliant, a tool must completely support SMM model elements. An implementation can provide:

- The capability to generate XMI documents based on the SMM XMI schema capturing measurements from the existing model of the tool.
- The capability to import measurements via representations based on the SMM XMI schema and to map the measurements into the existing model of the tool.

3 Normative References

The following normative documents contain provisions, which, through reference in this text, constitute provisions of this specification. For dated references, subsequent amendments to, or revisions of any of these publications do not apply.

- UML 2. Infrastructure Specification
- MOF 2.0 Specification

4 Terms and Definitions

We assume the following definitions:

Measure: A method assigning comparable numerical or symbolic values to entities in order to characterize an attribute of the entities.

Measurement: A numerical or symbolic value assigned to an entity by a measure.

Measurand: An entity quantified by a measurement.

Unit of Measure: A quantity in terms of which the magnitudes of other quantities within the same total order can be stated.

Dimension: A totally ordered range of values which can be stated as orders of magnitude relative to one another or to an archetypal member.

Measurement Accuracy: The measurement by which another measurement may be wrong.

Measurement Scope: The domain (set of entities) to which a given measure may be applied.

Measurement Range: The range (set of comparable values) assignable by a given measure.

5 Symbols

There are no symbols/abbreviations.
6 Additional Information

6.1 Changes to Adopted OMG Specifications
There are no changes to other OMG specifications.

6.2 How to Read this Specification
The rest of this document contains the technical content of this specification.

Although the chapters are organized in a logical manner and can be read sequentially, this reference specification is intended to be read in a non-sequential manner. Consequently, extensive cross-references are provided to facilitate browsing and search.

6.3 Acknowledgements
The following companies submitted and/or supported parts of this specification:

- EDS
- KDM Analytics
- Software Revolution
- Tactical Strategy Group
- NIST
- Benchmark Consulting
- eCube Systems

The following persons were members of the core team that designed and wrote this specification: Kevin Barnes, Djenana Campara, Larry Hines, Nikolai Mansurov, Alain Picard, John Salasin, Michael Smith, and William Ulrich.

7 SMM

Measurements provide data for disciplined software engineering in that engineers and their managers rely on these comparable evaluations in assessing the static and operational qualities of software systems.

Software measurement methods produce comparable evaluations of software or application artifacts. Counts such as number of screens, lines of code, and number of methods quantify the size of artifacts along a single dimension. These evaluations readily distinguish larger artifacts from smaller ones, likewise complexity metrics such as Halstead and Cyclomatic separate the simpler artifacts from the more complex. Comparable evaluations form mappings of artifacts of a given type into a single dimension.

Such is also the case for architecture measures (coupling and cohesion); functional measures (functions defined in system, persistent data as a percentage of all data, functions in current system that map to functions in target architecture); quality measures (failures per unit time, meantime to failure, meantime between repair); performance measures (average batch window clock time, average online response time); software assurance measures; and cost measures.
Predictive metrics provide a basis for continual system-level in contrast to fixed milestone-based assessments. These metrics may indicate at some future development stage the probability that the system will or will not meet its requirements.

This specification defines a meta-model for representing measurement related to existing software assets and their operational environments referred to as the Software Metrics Meta-model (SMM).

The SMM promotes a common interchange format that will allow interoperability between existing modernization tools, commercial services providers and their respective models. This common interchange format applies equally well to development and maintainence tools, services and models. SMM complements a common repository structure and so facilitates the exchange of data currently contained within individual tool models that represent existing software assets. Given that the repository’s meta-model represents the physical and logical software assets at various levels of abstraction as entities and relations, SMM represent the measurements of these assets.

The main goal for the SMM is to provide an extendable meta-model establishing a standard for the interchange of software-related measurements over the entities modeled by ADM Roadmap meta-models or other OMG meta-models. By software-related, we mean measurements derived from the existing software artifacts (including source, design and linkage from source to target architectures) or technical measurements concerning deployment. Source artifacts include program code, runtime traces, scheduling specifications, screen layouts and UML models. It may also include grid-service infrastructure descriptions and SOA adoption specification of multiple organization units in an enterprise.

SMM contains meta-model classes and associations to model measurements, measures and observations. We present and explain diagrams depicting measures, then measurements and finally observations.

SMM supports the meta-models of the ADM roadmap by providing quantifiable and specific indicators, in the form of counts, measures and computational results, about existing systems and the relationship of those systems to target architecture. The meta-model provides for and is extendable to measurements of entities modeled by other OMG meta-models where those measurements are software-related.

SMM avoids duplicating features of the measured artifact as features of the measurement. Consider as an example a log of bug reports. Possible measures are total bug count in the log, total time logged in the log and bugs per time-period. The unit of measures are a bug, a unit of time and bugs per time interval, respectively. SMM does not provide representations for bug, start time and end time. Their representations must be provided elsewhere.

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1 See OMG document admtf/04-09-02: Architecture-Driven Modernization Roadmap.
2 For example, the General Ledger Specification v1.0 provides representations for start_date and end_date.
A measurement result is precisely identified only if its measure is identified. To understand the meaning of 1000 lines we need to know that it is the result of measuring a program’s length in lines. The measured entity must be identified. That is, 1000 lines is for a particular program. Contextual information may also be needed. For example, function point counts of a program may vary depending upon the expert applying the measure.

Figure 1 presents the fundamental approach of this specification. Measurement has a value conveying the measurement results. The measurement may be of any MOF element as related by the measurand association. In this way, measurement is applicable to elements of other OMG meta-models including the Knowledge Discovery Meta-model and the Abstract Syntax Tree Meta-model. The measured entity may represent any software artifact or an aspect of an artifact.

The SMM associates an evaluation process, a measure, to each the measurement. Measures signify functions from the domain of software artifacts and aspects thereof to sets of ordered values.

Contextual information is related by Observation, such as who, where, and when. Observation may serve to distinguish distinct utilizations of a given measure on a given measurand.
8 Core Classes

8.1 SMM_Element Class (Abstract)

An SMM element constitutes an atomic constituent of a model. In the meta-model, SMM_Element is the top class in the hierarchy. SMM_Element is an abstract class.

Attributes

- name: String Specifies the name of the SMM element.
- description: String A detailed description for the element (optional).
8.2 SMM_Model Class

This class represents the aggregation of all the elements of the SMM.

8.3 SMM_Relationship (abstract)

This class is a model element that represents semantic association between SMM elements.

**SuperClass**

SMM_Element

**Associations**

- from:SMM_Element The *origin* element (also referred to as the from-endpoint of the relationship).
- to:SMM_Element The *target* element (also referred to as the to-endpoint of the relationship).

8.4 SMM_Category Class

This class represents categories of measures. A category has measures and other categories as its elements.

A category represents the measures directly associated with an ‘element’ and the measures of each sub-category likewise associated with an ‘element.’

A measure may appear in multiple categories. A category can be a subcategory of other categories indicating only that its measures also are measures of these other categories.

This class may be used to represent a family of similar measures which apply to different scopes such as lines of code in a file, lines of code in a method and lines of code in program. It may also represent a category of measures which are associated with a given software field or engineering task. For instance we speak often of Quality Assurance Metrics and Software Maintainability Metrics. The category of a metric may indicate the kind of purpose for which the metric is used.

- Environmental Metrics (e.g., number of screens, programs, lines of code, etc.)
- Data Definition Metrics (e.g., number of data groups, overlapping data groups, unused data elements, etc.)
- Program Process Metrics (e.g., Halstead, McCabe, etc.)
- Architecture Metrics (e.g., average call nesting level, deepest call nesting level, etc.)
- Functional Metrics (e.g., functions defined in system, business data as a percentage of all data, functions in current system that map to functions in target architecture, etc.)
- Quality Metrics (e.g., failures per day, meantime to failure, meantime to repair, etc.)
- Performance Metrics (e.g., average batch window clock time, average online response time, etc.)
- Software Assurance Metrics

Metric categorization has other uses as well. For example, measures may be categorized by tool support.
**Associations**

- categoryElement:Category Indicates that categoryElement is a subcategory of this category.
- categoryElement:Measure Indicates that measure is in this category.
- parameter:Category_Relationship[0..*] Associates parameters or features of the category.

### 8.5 Category_Relationship

This class is a model element that represents semantic or named association between SMM categories and other SMM elements. For example, a modeler may choose to create a “gold standard” measure for a selected category. To do so, the modeler can use a category relationship named “gold standard” to associate the measure to the category. See Figure 15.

**SuperClass**

SMM_Element

**Associations**

- from:SMM_Category Indicates the category which has relation.
- to:SMM_Element Indicates the SMM element related to the category.

**Semantics**

Category_Relationship represents a named association between a category and an element (SMM_Element) such as a measure.

### 8.6 Date

This represents dates. In a language binding it should be mapped to a type that allows ordered comparison. For XMI it is mapped to the XML Schema `date` type.

### 8.7 Timestamp

This represents a point in time: for example, a combination of a date and a time within the day. For XMI it is mapped to the XML `dateTime` type.
9 Measures

Measures are evaluation processes that assign comparable numeric or symbolic values to entities in order to characterize selected qualities or traits of the entities. Counting the lines of program code in a software application is one such evaluation.

There may be many measures that characterize a trait with differing dimensions, resolutions, accuracy, and so forth. Moreover, trait or characteristic may be generalize or specialized. For example, line length is a specialization of length which is a specialization of size.

Each measure has a scope, the set of entities to which it is applicable; a range, the set of possible measurement results; and the measurable property or trait which the measure characterizes. For example, the aforementioned line counting has software applications as one of its scope with line length as one of its measurable trait. Explicitly representing the scope and the measurable trait allows for the consideration of different measures which characterize the same attribute for the same set of entities. Each measurable trait may have multiple, identifiably distinct measures.

![Diagram of Measurable Characteristic and Scope]

Figure 3 Measurable Characteristic and Scope

The evaluation process may assign numeric values which can be ordered by magnitude relative to one another. These measures are modeled by the DimensionalMeasure class.

The evaluation process may alternatively assign numeric values which are percentages or, more generically, ratios of two base measurements. These measures are modeled by the Ratio class. The percentage of comment lines in an application exemplifies this type of measure.

The evaluation process may also assign symbolic values demonstrating a ranking which preserve the ordering of underlying base measures. These measures are modeled by the Ranking class. Cyclomatic reliable/unreliable criterion illustrates one such ranking. Reliable is comparably better than unreliable. Comparability is essential here because ranking is not intended to model every possible assignment of measurands.

The documentations of measures should stand by themselves so that an interchange of measurements may simply reference such documentation and not duplicate it.
9.1 Characteristic Class

This class represents a property or trait of the members in its scope, a set of MOF Elements, which may be characterized by applying a measure to those members. By specifying a characteristic a modeler is indicating what aspect, trait or property the measure purports to measure.

Note that Characteristic provides for a representation of a hierarchy of measures based upon the abstraction of measured trait. For example, a length characteristic may be the parent of the fileLength and programLength characteristics. programLength could be the parent of programLinesOfCodeLength.

SuperClass
SMM_Element

Attributes

name: String Specifies the name of the SMM element. (inherited)
9.2 Scope Class

This class represents sets of MOF::Elements as domains for measures. The domain is a subset instances of a class specified by the class attribute. If the subset does not include all instances of the given class then a restriction is specified either by enumerating the element or by specifying a recognizer for the subset elements.

The scope of a measure identifies a set of objects as the domain of the measure. The objects all exhibit to varying degrees the trait or property characterized by a measurement. SMM requires that the objects be instances of a single class. The set of objects may be further restricted by a recognizer function or by enumerating them explicitly. The recognizer and the enumeration are optional, but they cannot be used together.

The recognizer, if given, is a boolean function applicable to instances of the named class. The measure’s scope is restricted to those instances for which the recognizer returns true. Alternatively if enumeration is set then the scope is the set of instances (of the named class) associated as elements to the Scope.

SuperClass

SMM_Element

Attributes

class: String Specifies the class for elements of the set.
name: String Specifies the name of this entity set. (inherited)
enumerated: Boolean[0..1] If given and true, indicates that the elements of the set are enumerated by the element association.
recognizer:String[0..1] If given, provides a boolean operation applicable to instances of the class which returns true if and only if the instance is an element of the set.

Associations

element:MOF::Element[0..*] Specifies the elements of the set. Elements are specified if and only if enumerated is true.

Semantics

The class attribute may name a class within any OMG standard. The entities associated as elements of an Scope are restricted to members of specifies class.

9.3 Measure Class (abstract)

This class (see Figure 1) models the specification of measures either by name, by representing derivations of base measures, or by representing method operations directly applied to the measured object. The essential requirement for the measure class is that it meaningfully identifies the measure applied to produce a given measurement. For example, McCabe’s cyclomatic complexity could be specified by its name, McCabe’s cyclomatic complexity, by a direct measurement operation or by rescaling counts of either independent paths or choice points. A measure may alternatively be identified by citing a library of measure which includes the measure by name.
The scope of a measure identifies a set of objects as the domain of the measure. The objects all exhibit to varying degrees the trait or property characterized by a measurement. SMM requires that the objects be instances of a single class. The set of objects may be further restricted by a recognizer function or by enumerating them explicitly. The recognizer and the enumeration are optional, but they cannot be used together.

Scope need not be specified if the library and name are given. In that case, the scope can be found in the library.

A measure may be a refinement of another measure. The scope of the first measure is a subset of the second measure’s scope. The characteristic of both measures must be identical.

**SuperClass**

SMM_Element

**Attributes**

- **name:** String[0..1] Specifies the unique name of the measure. (inherited)
- **library:** String[0..1] Specifies library declaring measure.

**Associations**

- **equivalentFrom:** Measure[0..*] Indicates that two measures are equivalent.
- **equivalentTo:** Measure[0..*] Indicates that two measures are equivalent.
- **scope:** Scope Specifies a set of elements measurable by this measure.
- **refinement:** Measure[0..*] Specifies measures whose scopes are subclasses of this measure’s scope.
- **category:** SMM_Category[0..*] Specifies categories to which this measure belongs.
- **measurement:** Measurement[0..*] Indicates measurements obtained by this measure.
- **trait:** Characteristic Specifies the trait characterized by this measure.

**Constraint**

context Measure inv:
not library->isEmpty implies not name->isEmpty and scope->isEmpty implies not library->isEmpty.

**Semantics**

Assigning a measure to the equivalentTo role of another measure states that two measures are semantically indistinguishable. Any measurement result by one on a given entity under a given observation should equal a measurement by the other on the same entity and observation. The semantics of this association is symmetric, but only one direction needs to be given.

Throughout the remainder of this document we will say that a measure is a refinement of another measure if and only if the first is associated to the second as a refinement directly or transitively. This association implies that the class of the scope of a measure is a superclass of the class of the scope of any refinement measure. For any measure \( m \) and for any class \( c \) equal to \( m.refinement.scope.class \), \( c \) is the class or is a subclass of the class \( m.scope.class \).

The refinement association essentially establishes measures as methods of their scope’s classes.
9.4 MeasureRelationship (abstract)

MeasureRelationship is an abstract class representing any relationship between two measurements. See Figure 4. The class provides as an extension point.

SuperClass

SMM_Relationship

Attributes

name:String Specifies the name of this measure relationship. (inherited)

Associations

from:Measure Specifies the measure at the from endpoint of the relationship.
to:Measure Specifies the measure at the to-endpoint of the relationship.

9.5 DimensionalMeasure Class

This class models the specification of measures which assign numeric values that can be placed in order by magnitude. Dimensional measures have units of measures and their values span a dimension. See Figure 4.

The unit of measure is an archetypal or prototype element of the dimension. Every element of the dimension can be stated by a numerical multiple of the ‘unit of measure’ element.

The unit of measure does not distinguish between measures which share the same range. That distinction would be entirely within the purview of the measure identification. For examples, a height measure and a width measure may share the same unit of measure. That is to say, a measurement is not just a number and a unit of measure. The measured artifact must be indicated, the measure identified and contextual information retained as the observation.

SuperClass

Measure

Attributes

unit:String Identifies the unit of measure.

9.6 Ranking Class

This class represents simple range-based gradings or classifications based upon already defined dimensional measures. See Figure 4.
Examples are:

- Small, medium, large
- Cold, warm, hot
- A, B, C, D or F
- Reliable / Unreliable

Collectively the ranking intervals may completely cover the base dimension or may leave gaps. A base measurement in such a gap is considered unranked and is not representable as a measurement of the ranking measure.

The intervals may overlap. A ranking resulting in a particular symbol means and only means that the base measure resulted in a value occurring a ranking’s interval which mapped to that symbol. This does not exclude the possibility that the value might occur in another interval.

Ranking consists of mapping intervals to symbols where the intervals are parts of the underlying measure’s dimension. For example, 100 to 90 points maps to “A,” 80 up to 90 maps to “B,” 70 up to 80 maps to “C,” 60 up to 70 maps to “D,” and below 60 maps to “F.” The underlying dimension consists of grade points. The result is the usual A,B,C,D, and F style grade.

Ranking measure may represent a purely qualitative evaluation with no quantitative base measure. For example we could measure the non-standardness of the source language and evaluate it without quantification. It is identified as “2GL,” “Unacceptable 3GL or 4GL,” “Acceptable 3GL or 4GL,” or “Ideal Strategic Language.” The first two are judged equivalently non-standard. The third is more nearly standard and the last is standard.

**SuperClass**

Measure

**Associations**

- baseMeasure:DimensionalMeasure[0..1] Identifies the base measure on which this ranking measure is based.
- interval:RankingInterval[1..*] Identifies intervals within the dimension of the base measure and the symbol to which each interval is mapped.

**9.7 RankingInterval Class**

This class represents the mapping of an interval to a symbol which serves as a rank. The booleans, maximuOpen and minimumOpen, default to false. See Figure 4.

**SuperClass**

SMM_Element
Attributes

- maximumOpen:Boolean True if and only if interval include maximum endpoint.
- minimumOpen:Boolean True if and only if interval include minimum endpoint.
- maximum:Number Identifies interval’s maximum endpoint.
- minimum:Number Identifies interval’s minimum endpoint.
- symbol:String Base measurements within this interval are mapped by symbol.

Constraints

collection RankingInterval inv:
maximum ≥ minimum and (maximumOpen or minimumOpen → maximum > minimum)

SMM_Unit

10 Collective Measures

This diagram represents measures which assess container entities by accumulating assessments of contained entities which are found by the base measure. See demonstration given in Figure 6.

Most software engineering measures are collective. We count up lines of code for each program block and sum these values to measure routines, programs and eventually applications. A similar process is followed to count operators, operands, operator and operand occurrences, independent paths, and branching points.

Other frequently used container measures are based upon finding the maximum measurement of the container’s elements. Nesting depth in a program and class inheritance depth exemplify these collective measures.

The collective measure specifies the following measurement process:

1. Apply the base measure to each contained element to obtain a set of base measurements.
2. Apply the n-ary accumulator to the set of base measurements to obtain the measurement of the container.

Figure 6 demonstrates this process.
Figure 5 - Collective Measures
10.1 CollectiveMeasure Class

The CollectiveMeasure class represents measures which when applied to a given entity accumulates measurements of entities similarly related to the given entity. See Figure 5. For example, counts for container entities are often found by accumulating (adding) counts of the containers’ contained entities. In fact, sizing measures generally accumulate to containers by adding the results of applying the appropriate size measure to the contained entities.

Maximum is another frequent accumulator.

The measurands of the base measurements need not be the same of the measurand of the collective measurement. Within SMM, the measurands are just arbitrary MOF::Elements declared in another MOF model.

The SEI Maintainability Index is one such aggregation which does not change the unit of measure.
SuperClass
DimensionalMeasure

Attributes
accumulator:String Identifies the n-ary function which accumulates the base measurements.

Associations
baseMeasure:DimensionalMeasure The base measurements are derived by applying the specified measure or refinements of it.

10.2 AdditiveMeasure Class

AdditiveMeasure – a subclass of CollectiveMeasure which sums the measurements of the contained entities. See Figure 5.

SuperClass
CollectiveMeasure

Constraints
context MaximalMeasure inv:
accumulator = 'sum'

Accumulator is n-ary addition. If there are no contained entities then zero is returned by this measure.

10.3 MaximalMeasure Class

MaximalMeasure – a subclass of CollectiveMeasure which takes the maximum of the measurements of the contained entities. See Figure 5.

SuperClass
CollectiveMeasure

Constraints
context MaximalMeasure inv:
accumulator = 'maximum'.
10.4 DirectMeasure Class

DirectMeasure – a subclass of DimensionalMeasure which applies a given operation to the measured entity. See Figure 5.

SuperClass
DimensionalMeasure

Attributes

operation:Operation Specifies the measurement operation of this measure. It is applicable to elements of the class and returns numeric values interpretable with respect to the unit of measure.

10.5 Counting Class

Counting is a subclass of DirectMeasure where the given operation returns 0 or 1 based upon recognizing the measured entity. See Figure 5.

SuperClass
DirectMeasure

Constraints

context Counting::self.operation(...):int
post: result = 0 or result = 1

The operation is a recognizer which selects some subset of the elements of the measure’s scope found by self.scope. The recognizers returns 1 for the elements of the subset and returns 0 otherwise. Self.unit need not be an element of the subset.
10.6 BinaryMeasure Class

The BinaryMeasure class represents measures which when applied to a given entity accumulates measurements of two entities related to the given entity. See Figure 5. For example, areas for two dimensional entities are often found by accumulating (multiplying) lengths.

The measurands of the base measurements need not be the same as the measurand of the collective measurement.

**SuperClass**

DimensionalMeasure

**Attributes**

functor:String

Identifies the binary function which combines two base measurements.

**Associations**

baseMeasure1:DimensionalMeasure

The first base measurement is derived by applying the specified measure or a refinement of it.

baseMeasure2:DimensionalMeasure

The second base measurement is derived by applying the specified measure or a refinement of it.
Semantics

The usual semantics of algebra would require that the unit of a binary measure equals applying the accumulator to the units of the base measures. While conforming to this requirement would ensure more easily understood models, SMM does not enforce this requirement.

10.7 Ratio Class

This class represents those measures which are ratios of two base measures. See Figure 5. Examples include:

- Average lines of code per module,
- Failures per day,
- Uptime percentage – Uptime divided by total time,
- Business data percentage of all data,
- Halstead level = Halstead volume divided by potential volume,
- Halstead effort = Halstead level divided by volume.

A ratio measure and its two base measurements frequently characterize three different traits of the same entity. If the dividend characterized the total code length of an application and the divisor characterized the number of program in the application then the ratio characterizes the average code length per program.

Ratios may also characterize traits of distinct entities. For example, a ratio may contrast the code length between a pair of programs.

SuperClass

DimensionalMeasure

Constraints

context MaximalMeasure inv:
    functor = ‘divide’

11 Other Measures

The following diagram presents three additional measures.

- Direct applications of named measurements. (One such named measure is Cyclomatic Complexity.)
- Simple algebraic change of scales of already defined numeric measures (e.g., the translation to ‘choice points’ from Cyclomatic complexity).
11.1 NamedMeasure Class

The class allows for specifying measures which are well-known and can be specify simply by name. See Figure 8. For example, McCabe’s cyclomatic complexity. The meaning of applying the named measure should be generally accepted.

SMM is for the exchange of measurement results. To convey such results for well known measures, it suffices to identify the measure solely by name.

SuperClass

DimensionalMeasure

Attributes

name: String Specifies the name of the SMM element. This attribute is inherited from the Element class where it is optional. Here it is required.

Constraints

context NamedMeasure inv:
not self.name->isEmpty

11.2 RescaledMeasure Class

The measure specifies a process which re-scales a measurement on an entity with one unit of measure to obtain a second measurement of the same entity with an different unit of measure. See Figure 8.
SuperClass
DimensionalMeasure

Attributes

formula:String Specifies the algebraic formula which re-scales a result from the base measure’s dimension to obtain a value expressed in a different unit of measure with respect to this measure’s unit of measure

Associations

baseMeasure:DimensionalMeasure Identifies the measure applied to each “contained” entity to determine base measurements.

12 Measurements

Measurement results are values from ordered sets. Such a set may be nominal (e.g. Poor, Fair, Good, Excellent) as long as there is an underlying order. A set may instead define a dimension where its values may be stated in orders of magnitude with respect to archetypal member. SMM allows for dimensional measurements. The magnitude is the measure’s unit of measure.

SMM also allows for dimensionless measurements derived by ratios and ranking schemes. In the former the ratio is derived from two measurements of the same dimension; whereas, in the latter measurements from a dimension are mapped to symbolic representations (e.g., 100-90 becomes “A,” 89-80 becomes “B”).

The modeling of measurements mirrors the modeling of measure.

Figure 9 - Measurements
12.1 Measurement Class (abstract)

The Measurement class represents the results of applying the associated Measure to the associated Measurand. See . Two measurements of the same measurand by the same measure can be distinguished by observation information provided by the associated Observation.

Measurand is in the scope of the measure.

The value of a measurement is an element of an ordered set. It may be a number where the ordering is the usual standard. The DimensionalMeasurement and Percentage subclasses of Measurement defined below have numeric values. The value may also be a symbol that we can map to a numeric interval. The Grade subclass has a symbolic value.

Measure is a process and, hence, may fail. The error attribute of measurement allows such failures to noted. A measurement either has a value or an error is recorded.

**SuperClass**

SMM_Element

**Attributes**

- error:String[0..1] If an error occurred in the measurement process, this field contains a code representing the error.

**Associations**

- measure:Measure Identifies the process by which the measurement was determined.
- measurand:MOF::Element Identifies the object measured.
- observation:Observation Provides contextual information which may distinguish this measurement from other assessments by the same measure on the same measurand.

**Semantics**

Measurand must be in the scope of measure. Specifically, measurand must be an instance of the class named in measure.characterizes.scope.class. If class named in measure.characterizes.scope.enumerated is true then measurand is associated as an element to class named in measure.characterizes.scope. Otherwise, if measure.characterizes.scope.recognizers is given then the recognizer applied to the measurand must return true.

If the measure is identified by name and library, then the measure’s measurable trait need not appear when convey of measurement. In that case the definitive measure is given in the named library with the given name. The measurable trait is found in the library by following the associated characterizes role.

12.2 MeasurementRelation (abstract)

MeasurementRelation is an abstract class representing any relationship between two measurements. See Figure 9.
12.3 DimensionalMeasurement Class

The DimensionalMeasurement class represents the results of applying a dimensional measure to an entity. The result is given in terms of the measure’s unit. See Figure 9.

Attributes

value:Number[0..1] Represents the measurement result as a magnitude with respect to the unit of measure.

Constraints

context DimensionalMeasurement inv:
measure.oclIsTypeOf(DimensionalMeasure) and error->isEmpty <> value->isEmpty

12.4 Grade Class

The Grade class represents the grade found by Ranking measure. Its ranking scheme mapped the grade’s underlying base measurement to the grade’s symbol. Once again, the base measurements shares its measurand with this derived gradingis. See Figure 9.

Attributes

value:String[0..1] Identifies rank as a measurement derived from the base measurement.

isBaseSupplied:Boolean True if baseMeasurement is supplied.

Associations

baseMeasurement:DimensionalMeasurement[0..1] Identifies the measurement from which the rank was derived.
Constraints

context Grade inv:
measure.oclIsTypeOf(Ranking) and
error->isEmpty <> value->isEmpty and
isBaseSupplied \rightarrow (measurand = baseMeasurement.measurand and
baseMeasurement.measure = measure.baseMeasure)

Semantics

If isBaseSupplied holds, then value is one of the symbols found by measure.interval where baseMeasurement.value is in
the interval. A numeric value is in the interval if and only if the it is less than the maximumEndPoint when
maximumOpen is false, less than or equal to maximumEndPoint when maximumOpen is true, greater than
minimumEndPoint when minimumOpen is false, and greater than or equal to minimumEndPoint when minimumOpen is
ture.

Figure 10 - Grade Constraint

13 Collective Measurements

This class represents measurements found by accumulating a set of base measurements. For example, the number lines
of code in application can be determines by accumulating the number lines in its programs.
13.1 CollectiveMeasurement Class

The CollectiveMeasurement class represents the results of applying its CollectiveMeasure measure to an entity. See Figure 11. In this case, applying the measure is as follows:

1. Apply the base measure to each contained element to obtain a set of base measurements.
2. Apply the n-ary accumulator to the set of base measurements to obtain the measurement of the container.

The results of step 1 are the DimensionalMeasurements associated by base measurement.

**SuperClass**

DimensionalMeasurement

**Attributes**

- isBaseSupplied:Boolean True if baseMeasurements are supplied. All are supplied or none is assumed.
- accumulator: Accumulator Enumerated value indicating the type collective measure
Associations

baseMeasurement:DimensionalMeasurement[0..*]  Identifies the measurements from which this collective measurement was derived.

Constraints

context CollectiveMeasurement inv:
measure.oclIsTypeOf(CollectiveMeasure) and
isBaseSupplied →
(not baseMeasurement->isEmpty and baseMeasurement.measure=measure.baseMeasure)

Semantics

If isBaseSupplied holds, then value equals the result of applying measure.accumulator the set of values given by baseMeasurement.value.

13.2 DirectMeasurement Class

The DirectMeasurement class represents the measurement results found by of applying the measure’s specified operation directly to the measurand. See Figure 11.

SuperClass

DimensionalMeasurement

Constraints

context DirectMeasurement inv:
measure.oclIsTypeOf(DirectMeasure)

13.3 Count Class

Counting forms the basis for multiple software metrics. This class consists of a particular subclass of directMeasurement which is very useful in counting. See Figure 11. Its associated measure is a CountingMeasure where the specified operation is a recognizer operation. Therefore, the value of any instance of this class is 1 or 0 depending upon whether or not the measurand is recognized.

SuperClass

DirectMeasurement

Constraints

context Count inv:
measure.oclIsTypeOf(CountingMeasure)
13.4 BinaryMeasurement Class

SuperClass

DimensionalMeasurement

Attributes

isBaseSupplied:Boolean True if both base measurements are supplied.

Associations

baseMeasurement1:DimensionalMeasurement[0..1] Identifies the first base measurement.
baseMeasurement2:DimensionalMeasurement[0..1] Identifies the second measurement.

Constraints

context RatioMeasurement inv: measure.oclIsTypeOf(BinaryMeasure) and isBaseSupplied →
(not baseMeasurement1.isEmpty and not baseMeasurement2.isEmpty) and
(not baseMeasurement1.isEmpty →
(baseMeasurement1.measure = measure. baseMeasurement1) and
not baseMeasurement2.isEmpty →
(baseMeasurement2.measure = measure. baseMeasurement2)

Semantics

If isBaseSupplied holds, then value equals the result of applying measure.functor to baseMeasurement1.value and baseMeasurement2.value.

13.5 RatioMeasurement Class

The RatioMeasurement class affords evaluations of a ratio measure of two evaluations of different dimensional measures. See Figure 11. The measure associated with the dividend has its unit of measure in common with the measure associated with the divisor.

SuperClass

BinaryMeasurement

Constraints

context RatioMeasurement inv: measure.oclIsTypeOf(RatioMeasure) and isBaseSupplied → (value = baseMeasurement1.value / baseMeasurement2.value)
14 Named and ReScaled Measurements

Measurement is in terms of its unit of measure as specified under its associated DimensionalMeasure. That is, the measurement is a multiple of its unit of measure where value determines the multiple.

![Diagram of measurement classes]

Figure 12 - Named and ReScaled Measurements

14.1 AggregatedMeasurement Class

The AggregatedMeasurement class represents the measurement results of applying the operation specified by the measure to the base measurements. See Figure 12. Its measurand and the measurand of its base measurement are identical. That is, this is not a measurement of a container as represented by the CollectiveMeasurement. Instead, AggregatedMeasurement combines different measurements of a given entity to create a new measurement for that entity. The SEI Maintainability index demonstrates this process.

\[
171 - 5.2 \ln(\text{aveV}) - 0.23(\text{aveV}(g')) - 16.2(\ln(\text{aveLOC})) + 50(\sin(\sqrt{2.4(\text{perCM})}))
\]

**SuperClass**
DimensionalMeasure

**Attributes**

isBaseSupplied:Boolean
True if base measurements are supplied. All are supplied or none is assumed.
Associations

baseMeasurement:DimensionalMeasurement[0..*]  Identifies the measurements from which this aggregated measurement was derived.

Constraints

context AggregatedMeasurement inv:
measure.oclIsTypeOf(AggregatedMeasure) and
isBaseSupplied  → (not baseMeasurement->isEmpty) and
forAll(b:baseMeasurement | b.measure = measure.baseMeasure)

Semantics

If isBaseSupplied holds, then value equals the result of applying measure.accumulator the set of values given by baseMeasurement.value.

14.2 NamedMeasurement Class

The NamedMeasurement class represents the measurement results of applying to the Measurand measurement processes which are generally known and identifiable by name. See Figure 12.

SuperClass

DimensionalMeasure

Constraints

context NamedMeasurement inv:
measure.oclIsTypeOf(NamedMeasure).

14.3 ReScaledMeasurement Class

The ReScaledMeasurement class represents the measurement results of applying to the base measurement the operation specified by the Measure to rescale the measurement. That is, given a one measurement of the measurand with respect to one unit of measure, we obtain a second measurement of the measurand with respect to a different unit of measure. See Figure 12.

Measure is a RescaledMeasure.

SuperClass

DimensionalMeasure

Attributes

isBaseSupplied:Boolean  True if the base measurement is supplied.
**Associations**

baseMeasurement:DimensionalMeasurement[0..1]  Identifies the measurement from which this measurement was derived.

**Constraints**

class ReScaledMeasurement inv:
measure.oclIsTypeOf(RescaledMeasure) and
isBaseSupplied \rightarrow
not baseMeasurement->isEmpty and baseMeasurement.measure = measure.baseMeasure

**Semantics**

If isBaseSupplied is true then value equals result of applying measure.operation to the baseMeasurements’ values.

### 15 Observations

Measurements are sometimes repeated. An old carpentry rule is measure twice, cut once. To distinguish these multiple measurements, the observation class can represent contextual information such as the time of the measurement and the identification of the measurement tool.

**Figure 13 - Observations**

#### 15.1 Observation Class

This class represents some of the contextual information which may be unique to this measurement such as date, measurer and tool used. See Figure 13.

**SuperClass**

SMM_Element

**Attributes**

- whenObserved: Date[0..1]  Identifies the “moment” when the measurement was taken.
- observer: String[0..1]  Identifies measurer.
- tool: String[0..1]  Identifies tool used in measurement.
16  Historic and Trend Data (Non-Normative)

SMM does not model tracking or trend data directly. Linking versions of objects through a software evolution poses a concern in modeling software evolution even if measures are never taken. When the measurand’s model provides the linkage (e.g. an “EvolvesTo” relationship), then a measurement of an original artifact could be traced to its newer versions and to their measurements if available. The diagram below (Figure 14) is overly simplistic, but hopefully conveys the gist of such tracing. The beige filled instances indicates the metric representations augmenting the base model (green). The central point is that the evolves path is between instances of the base model. The measures of the evolving artifacts can be gathered or compared only if the linkage between the artifacts is captured and maintained through the modeling of the system development and modification.

![Diagram](image)

Figure 14 - Tracking Measurements Across Versions

17  Inaccuracy (Non-Normative)

Inaccuracy of a measurement is the amount by which the measurement is in error. That is, we may model inaccuracy as measure if we first model a measure which is assumed to be true. Inaccuracy of a measurement is then just the difference between the measurement and a “true” measurement of the same entity.

In SMM inaccuracy is representable by measures which characterizes inaccuracy. The measures are comparable elevation of measurements evaluated by the difference between the measurement and the truest (at least accepted as such) measurement of that entity for that trait.
Given two measures which characterize the same trait and share the same scope, then inaccuracy can be modeled as

In the demonstration below (Figure 15), a category collects measures which are applicable to ExampleClass1 and characterize ExampleTrait. The category identifies the “truest” measure by the goldStandard relationship and identifies an appropriate inaccuracy measure for Measure1 by the InaccuracyMeasure relationship.

A Characteristic may have a measure which is designated as the best or truest measure of the attribute. That measure may be associated as the attribute’s gold standard. Such a designation allows for the representation of inaccuracy for each of the attribute’s measures as the difference between the measure and the gold standard.

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**Figure 15 - Inaccuracy Demonstration**

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Software Metrics Meta-Model, Beta 1
Figure 16 - Uncertainty Demonstration

Figure 17 - SMM Extension for Uncertainty
18  Library of Measures (Non-Normative)

The following is a suggestive list of measurement classes along with their measure classes and measurand classes. Sources include:

- *Comsys Systems Redevelopment Methodology:*
  www.comsysprojects.com/SystemTransformation/TMethodology.htm

Each measure is defined using the classes of the SMM. The referenced software artifacts are modeled using the Knowledge Discovery Metamodel (KDM) unless otherwise noted.

18.1 Various Counts

18.1.1 Module Count\(^3\)

Module Count ≡ A count of the number of modules in a system.

Assume that the system is modeled by a KDM model. The KDM:AbstractCodeElement serves as a container of code parts as well as modeling the code parts themselves. The KDM:Module is an AbstractCodeElement subclass which models modules. See Figure 18.

Counting the modules in the code model requires summing the results of a recognizer for module across the model. The unit of measure is module. See Figure 19 for the library entry and see Figure 20 for a brief demonstration.

\(^3\) See GAM 003 in Comsys Systems Redevelopment Methodology.
Figure 18 - KDM Code Package Fragment
Figure 19 - Library Entry for Module Count in Code Model

Figure 20 - Module Count in Model Demonstration
Counting the modules in an abstract code element sums recursively the count up the code part hierarchy.

It requires noticing if the code element is a module and returning 1 as well as recursively counting the modules in all the contained code elements. This is a CollectiveMeasure which sums two base measures. The first is a CountingMeasure which recognizes modules. The second is a sum accumulator of the owner/codeElement association from CodeElement to CodeElement and its base measure is the above CollectiveMeasure. The unit of each of these measures is a module.

For the entire system, we count the modules in the CodeModel which owns the top-level code elements of the system. The counting is a CollectiveMeasure with a sum accumulator of the model/codeElement association from CodeModel to CodeElement and its base measure is the above counting of modules in a code element.

### 18.1.2 Screen Count

Screen Count ≡ A count of the number of screens in a system.

![Figure 21 - KDM Action Package Fragment](image-url)

Figure 21 - KDM Action Package Fragment

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4 See TEM 153 in Comsys Systems Redevelopment Methodology.
Assume that the system is modeled by a KDM model. The KDM:UIElement serves as a container of user interface parts as well as modeling the user interface parts themselves. The KDM:Screen is a UIElement subclass which models screens.

Count the screens in a code element requires noticing if the user interface element is a screen and returning 1 as well as recursively counting the screens in all the contained user interface elements. This is a CollectiveMeasure which sums two base measures. The first is a CountingMeasure which recognizes screens. The second is a sum accumulator of the
owner/UIElement association from UIElement to UIElement and its base measure is the above CollectiveMeasure. The unit of each of these measures is a screen.

For the entire system, we count the screens in the UIModel which owns the top-level user interface elements of the system. The counting is a sum accumulator of the model/uiElement association from UIModel to UIElement and its base measure is the above counting of screens in a user interface element. The unit of measure is “each”.

18.1.3 Method Count

Method Count ≡ A count of the number of methods in a system.

Figure 24 Method Count Library Entry

Figure 25 - Method Count Demonstration
Assume that the system is modeled by a KDM model. The KDM:MethodUnit is a CodeElement subclass which models methods. The counting of methods then is very similar to the counting of modules given above.

Counting the modules in a code element requires noticing if the code element is a method and returning 1 as well as recursively counting the methods in all the contained code elements. This is an CollectiveMeasure which sums two base measures. The first is a CountingMeasure which recognizes methods. The second is a sum accumulator of the owner/codeElement association from codeElement to codeElement and its base measure is the above CollectiveMeasure. The unit of each of these measures is a method.

For the entire system, we count the methods in the CodeModel which owns the top-level code elements of the system. The counting is a sum accumulator of the model/codeElement association from CodeModel to CodeElement and its base measure is the above counting of modules in a code element. The unit of measures is a method.

18.1.4 Lines of Code

A line of code is any line of program text that is not a comment or a blank line, regardless of the number of statements or fragments of statements on the line. This specifically includes all lines containing program headers, declarations, and executable and non-executable statements. Lines of code here means fully expanded lines of code including copy books, includes, and comments.

KDM does not directly model lines of source, code or otherwise. As a demonstration, let us assume that blank lines may be included. This allows us to use the KDM SourceRegion to measure lines of code. We will further assume source region do not overlap or even having one start on the line that another ends on. The problem here is that code snippets are the smallest pieces of source modeled in KDM. Lines by themselves are not which means counting them is indirect. We will sum of the line size of code snippets and call that counting lines of code.

Lines of SourceRegion and SourceRef

KDM specifies a code snippet with a SourceRegion element which have two attributes, startLine and endLine, that interest us here. The number of lines in the SourceRegion is endLine – StartLine + 1.

Our representation is a DirectMeasure with a class of SourceRegion and a function of endLine – startLine + 1.

SourceRef consists of multiple SourceRegions. Assuming no overlap as stated above, the determination the lines of code in a SourceRef is an AdditiveMeasure with the previous lines of SourceRegion as its base measure.

Figure 26 Lines of Code Measures

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5 See ERP 001 in Comsys Systems Redevelopment Methodology.
Figure 27 - Lines of Code Demonstration

Lines of AbstractCodeElement

Figure 28 - Additional Lines of Code Measures
Refinement of Lines of ControlElement, CodeElement and Module

The source role for these elements is SourceRef. Determining the lines of code in each is an AdditiveMeasure where the base measure is the lines of SourceRef given above.
Figure 30 - Module LOC Demonstration

Figure 31 - Comment Line Count
18.1.5 Lines of Code for ASTM

The Abstract Syntax Tree Metamodel (ASTM) facilitates the interchange of programming language constructs parsed as abstract syntax trees. The Generic Abstract Tree Metamodel establishes a common core for modeling across a wide variety of programming languages. Each of these constructs may, of course, be measured by their lines of code.

GASTM does not directly model lines of source, code or otherwise. We will, consequently, make the same assumptions we made above for KDM. Blank lines are included and overlaps are ignored.

Figure 32 shows a fragment of the proposed ASTM covering the core syntax object, source location and source file. Figure 33 shows a possible SMM library entry to represent lines of code measure of GASTM syntax objects.

18.2 McCabe

McCabe’s cyclomatic complexity could modeled as a NamedMeasure. It is widely recognized. Alternatively, it could be a ReScaledMeasure from count of independent paths found by adding 2. Another representation would be as aReScaledMeasure from count of branching points found by adding 1. Each of these representations are present equivalent measures. We demonstrate below cyclomatic as a NamedMeasure and as a ReScaledMeasure from branching factor.
18.2.1 Branching Factor of ActionElements and Modules

Branching Factor is simply the difference between the number of nodes and edges in a module’s control flow graph. KDM models the nodes as ActionElements, the edges as ControlFlow. Branching factor is then measured by subtracting the count of ControlFlow instances from the count of ActionElements.

Figure 34 - Control Flow Edge Count Library Entry

Figure 35 - Control Flow Node Count Library Entry
18.2.2 Cyclomatic Complexity of a Module

Cyclomatic complexity (CC) = \( E - N + p \) where \( E \) is the number of edges of the flow graph, \( N \) is the number of nodes of the flow graph and \( p \) is the number of connected components.

In this demonstration we assume that the control graph of each module is entirely connected. That is, \( p \) is always 1. Cyclomatic is then simply the branching factor of a module plus one.

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7 See TPM 065 in Comsys Systems Redevelopment Methodology.
18.2.3 Extended Cyclomatic Complexity of a Module

Extended cyclomatic is the count of predicates or atomic formula in the condition of branching statements. We demonstrate this count based upon ASTM modeling of an “if” statement. The condition of the “if” is an expression which can be navigated to find its atomic formulas.

18.2.4 Average Extended Cyclomatic Complexity of Modules in the System

Ratio of Additive ECC over Additive Counting of modules.

18.2.5 Counts of Operating Systems

The Application Management and System Monitoring for CMS Systems (ASMS) specification provides a PIM based upon commercial enterprise management called the DMTF Common Information Model (CIM). “CIM models a software or hardware system as a collection of component models connected via associations. A specific instance of a system is modeled as a collection of instances of component models and associations.”

We demonstrate the counting of operating systems installed and running on computer systems.

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9 See dtc/07-05-02.
Figure 38 - ASMS Fragment
Figure 39 - OS Counting Demonstration
18.3 Halstead

18.3.1 Distinct Operator Count of a Module

\[ \eta_1 \equiv \text{A count of the number of distinct operators in a module.} \]

Distinguishing operators invocations from calls to externally defined routines is not the type of higher level architectural concerns represented in the KDM. Counting the number of called, but not defined elements would get us close to this metric.

18.3.2 Distinct Operand Count of a Module

\[ \eta_2 \equiv \text{A count of the number of distinct operands in a module.} \]

This is the data count shown above.

18.3.3 Operator Occurrence Count of a Module

\[ N_1 \equiv \text{A count of the number of operator occurrences in a module.} \]

This is a count of the calls to elements identified as operators.

18.3.4 Operand Occurrence Count of a Module

\[ N_2 \equiv \text{A count of the number of operand occurrences in a module.} \]

For KDM, this is a count StorableElements owned by ActionElements.

18.3.5 Halstead Length of a Module

\[ N = N_1 + N_2 \]

This is an CollectiveMeasure where the aggregator is addition and the base measures are the occurrence counts given above.

18.3.6 Halstead Vocabulary of a Module

\[ \tilde{\eta} = \eta_1 + \eta_2 \]

This is an CollectiveMeasure where the aggregator is addition and the base measures are the counts given above.

18.3.7 Halstead Volume of a Module

\[ V = N \log_2 \tilde{\eta} \]
First log, $\eta$ is a ReScaledMeasure based upon the vocabulary metric given above. The volume is then an CollectiveMeasure of the length given above and the rescaled vocabulary with multiplication as the aggregator. The unit of measure for the rescaled vocabulary and for the volume is “required bits of representation.”

**Figure 40 - Halstead Vocabulary Library Entry**
Figure 41 - Halstead Volume Library Entry
Figure 42 - Halstead Potential Library Entry
Figure 43 - Halstead Effort Library Entry
18.4 Software Engineering Institute (SEI) Maintainability Index

$$171 - 5.2(\ln(\text{aveV})) - 0.23(\text{aveV}(g')) - 16.2(\ln(\text{LOC})) + 50(\sin(\sqrt{2.4(\text{perCM})}))$$

Each of the averages are RatioMeasures of their respective metric (V for Halstead volume, V(g’) for extended Cyclomatic complexity and LOC of line of code) for modules over the count of modules. perCM, the percentage of comments in a module, is a PercentageMeasure of line count of comments over the total line count of a module.

Each resulting metric is rescaled to share the same unit of measure, namely maintainability index points.

<table>
<thead>
<tr>
<th>Metric</th>
<th>Rescaling Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>aveV</td>
<td>$50 - 5.2(\ln(\text{aveV}))$</td>
</tr>
<tr>
<td>aveV(g’)</td>
<td>$50 - 0.23(\text{aveV}(g'))$</td>
</tr>
<tr>
<td>aveLOC</td>
<td>$21 - \ln(\text{LOC})$</td>
</tr>
<tr>
<td>perCM</td>
<td>$50(\sin(\sqrt{2.4(\text{perCM})}))$</td>
</tr>
</tbody>
</table>

The SEI index is then an CollectiveMeasure for a module of the above four rescalings with addition as the aggregator.
Figure 45 - Conversion of Information Size to Maintainability
Figure 46 - Conversion of McCabe Cyclomatic to Maintainability
Figure 47 - Conversion of LOC to Maintainability
Figure 48 - Conversion of Comment Count to Maintainability
18.5 Qualitative Example

18.5.1 Non-standard language usage score

Non-standard languages are defined by an organization’s accepted technology standards. Assign the following scores where a 1 or 2 is low, a 3 is medium and a 5 is high:

1. 2GL or unacceptable 4GL assign 1 or 2
2. Acceptable 3GL or 4GL assign 3 or 4
3. Ideal strategic language assign 5
19 Library of Categories

SMM does not establish a standard set of measurement categories which presents an organization of measures applicable to every software environment, every stage of software life cycle, every software platform, software language or every software engineering activity. SMM minimally establishes a demonstration library of metric categories. The library does not assert that the given categories are standards. These metric categories reflect a high-level summary of industry metrics that support some software engineering processes.

19.1 Environmental Metrics

number of screens, programs, lines of code, etc.

19.2 Data Definition Metrics

number of data groups, overlapping data groups, unused data elements, etc.
19.3 Program Process Metrics
Halstead, McCabe, etc.

19.4 Architecture Metrics
average call nesting level, deepest call nesting level, etc.

19.5 Functional Metrics
functions defined in system, business data as a percentage of all data, functions in current system that map to functions in target architecture, etc.

19.6 Quality / Reliability Metrics
failures per day, meantime to failure, meantime to repair, etc.

19.7 Performance Metrics
average batch window clock time, average online response time, etc.

19.8 Security / Vulnerability
breaches per day, vulnerability points, etc.